DAMAGED GOODS

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price discriminate. Many instances of this phenomenon are observed. It may Manufacturers may intentionally damage a portion of their goods in order to result in a Pareto improvement.

• INTRODUCTION

rior to the 486DX but more expensive to produce. Nevertheless, in half the price of the chip that is less expensive to produce (Frenkel, 1991, the 486DX sold for \$588, and the 486SX for \$333, a little over then disabled the math coprocessor, to produce a chip that is strictly infecurious way. Intel began with a fully functioning 486DX processor, The 486SX processor of Intel Corporation was initially produced in a

can sell to customers who do not value the superior product so much, crimination. By producing an inferior substitute, the manufacturer production. The obvious reason for doing so is to permit price disand that many manufacturers intentionally damage a portion of their without decreasing demand for the superior product very much.² The We will argue in this paper that this is not an isolated incident,

We thank Bruce Smith, Hal Varian, and seminar participants at Cornell, Harvard, Michigan State, Montreal, NYU, Northwestern, Princeton, Rice, SMU, Texas, Washington, and Yale for helpful discussions.

1. The phenomenon is sufficiently well known among marketing professionals that it has a name: *crimping the product*.

2. Most authors agree that it is possible to price discriminate with differentiated products, by charging distinct markups on the goods. For example, Jean Tirole (1988, p. 134) argues that "It should not be inferred that price discrimination does not occur when differentiated products are sold to different consumers," and specifically cites

that damaging the superior product is the least expensive way to progood may be a less expensive way to produce a low quality good than directly manufacturing the low quality good. Indeed, we presume novelty of this paper is not in noting that damaging a high quality benefit from the price discrimination. improvement: the manufacturer and all types of consumers strictly duce the inferior product. Our insight is that this may be a strict Pareto

mand consumers prefer the high quality good. In order to introduce ity good, but if the prices were slightly closer together, the high dechasing the low quality good, respectively. Further suppose that at chasing the high quality good, and the low demand consumers purrepresent the monopoly prices for the high demand consumers purgood to the low demand types, the low demand types obviously benehigh quality good, chooses to sell only to the high demand types types of consumers. Suppose that a manufacturer, selling only the between the two monopoly prices. the low quality good, then, the manufacturer must reduce the gap these prices, the high demand consumers would prefer the low qualfit. Why may the high demand types benefit as well? Let M_H , M_I When the manufacturer price discriminates and sells a low quality The simplest way to see the welfare effects is in the case of two

increase M_L slightly. Note that low demand consumers still benefit its, the profit maximizing way to narrow the gap is to reduce M_H and introduces the low quality good when profits increase, the very exiscompared to not being served at all. Finally, as the manufacturer only from introducing the damaged good, because the increase in M_L is Since there is a zero first-order effect from reducing M_H on prof-

tence of the good tells us that profits go up.

This paper adds to a standard result—that if price discrimination permit free resale, limiting the manufacturer to the more common ways. First, the standard result assumes no resale. expands output, then a welfare improvement tends to occur-In contrast,

the example of quality differentiated services. In our context, the case for price discrimination is compelling. At lower cost, the manufacturer could have sold the high quality good, but instead chose to damage a portion of production, in order to be able to charge a lower price on the product. Thus, it is as if the manufacturer were selling the high quality product at two distinct prices—one without damage, and one with. This would not be price discrimination if the manufacturer's costs on the damaged good were lower, but since the manufacturer has incurred costs to damage the good, the manufacturer has incurred costs to damage the good, the manufacturer has incurred costs to damage the good. turer must be discriminating.

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tion a strict Pareto improvement for all types. 4 case for a Pareto improvement, in some cases making price discrimina-Second, case of second degree (incentive compatible) price discrimination.³ incentive compatible price discrimination strengthens the

cluding remarks involves a continuum of consumers with different reservation prices only one use for the product, such as the 486 chip, the natural model the dual use environment is analyzed in Section 3. When there is markets correspond to distinct groups of software users. A model of are two types of consumers; for example, the educational and business distinct uses for the product, the natural model is one where there and those where there is only a single use for the product. With two categories: those where there are two distinct uses for the product, a number of examples of manufacturers intentionally damaging a por-We analyze this case in Section 4. We end the paper with some conof their production. These examples divide naturally into two The paper is organized as follows. In Section 2, we will present

2. DAMAGED GOODS

and provide a brief summary of a variety of other examples enhancing their discriminatory abilities. We document four examples, out history and across a broad variety of different industries, manufaction of their production? In this section, we will argue that, throughturers damage some of their production solely for the purpose of How common is it for manufacturers to intentionally damage a por-

our paper states conditions on the demand primitives (rather than conditions on endog-3. The most general results known to date (Varian, 1985), while phrased in terms of third degree price discrimination, do allow for demand interdependencies, and hence could be applied to demand structures derived from self-selection models. However, enous variables) and focuses on Pareto improvements (rather than mere welfare in-

that incurring costs in order to damage production may make everyone better off, and that this is a quite plausible outcome in the dual use case, while a less plausible outcome in the single use case. an incentive compatible price menu, so that buyers self-select into categories by their choice of good to purchase. While it is known that net welfare gains can be obtained In contrast, we consider the case of second degree price discrimination, where the seller does not condition on observable characteristics of the buyers, but instead offers results in a Pareto improvement. However, because of the absence of demand interdethat Pareto improvements may arise, nor investigated the circumstances that tend to lead to Pareto improvements. The main theoretical contribution of our paper is to prove in the case of second degree price discrimination, to our knowledge, no one has shown pendencies, the high demand market obtains the same price and utility as in the absence of price discrimination; the Pareto improvement arises because a new market is served. Varian (1985) constructs an example where third degree price discrimination

2.1 THE 486SX

steps on a 386. Second, it contains an 8 kilobyte internal cache memspeeds (operations per second). performs a 386-387 combination, even when running at lower clock series. The combined effects of these improvements is that a 486 outbetween the processor and the coprocessor, as occurred with the 386 the same microprocessor eliminates time consuming communication floating point numerical computations. Installing the coprocessor in that it contains a 387 compatible math coprocessor, which handles them from slower external DRAM. The final advantage of the 486 is ory, allowing the 486 faster access to instructions than if it had to fetch forming some operations in one step that would have taken several First, it makes more efficient use of internal clock cycles, thereby per-The 486 microprocessor improved on the 386 in a number of ways. nificant improvement in performance over its predecessor, the 386. With the introduction of the 486 microprocessor, Intel provided a sig-

original 486 the 486DX. Unlike the 386SX processor⁵ after which it high performance alternative to the 386: the 486SX. Intel renamed the petitor Advanced Micro Devices, Intel decided to introduce a low cost, In response to fast 386 based microprocessors produced by com-

abled. (Frenkel, 1991) important differencethe 486SX is an exact duplicate of the 486DX, with one -its internal math coprocessor is dis-

387SX, however, the 487SX is not a real coprocessor. with the 386, it is possible to improve numerical calculations on a 486SX by purchasing the 487SX math "coprocessor." 1991 for substantially less: \$333 as opposed to \$588 for the 486DX. As Although it is more costly for Intel to produce the 486SX, it sold in Unlike

coprocess at all. It simply disables the 486SX processor and the 487SX is really a 486DX. . . . In fact, the 487SX doesn't is actually a 486DX with the FPU disabled. So in reality, ing-point unit (FPU) enabled. Keep in mind that the 486SX performs like the 486DX that it really is. (Frenkel, 1991) The 487SX math coprocessor is really a 486SX with the float-

^{5.} The 386SX was a 386 with a smaller internal data bus, which allowed PC manufacturers to use the 386SX as a "drop-in" replacement for the previous standard 286, without having to redesign the computer for the 386, yet increasing power and compatibility with the 386 generation of chips.

operation of the 486SX. coprocessor, is actually a fully functioning 486DX that disables the the equivalent of two 486DX microprocessors: one with its internal owner of a 486SX based personal computer must therefore purchase To obtain the full capabilities of a 486DX based machine, an purposely disabled, and one that, while labeled a

sells the 487SX at \$799, significantly more than the 486DX. chase a 487SX alone even if it did work without the 486SX, for Intel ability is actually used. Moreover, it would not be economic to purence of the 486SX to operate, although none of the 486SX's processing processor, because Intel designed the 487SX so that it needs the pres-It is not possible to purchase a 487SX and use it as a standalone

so that the SX socket won't accept the 486DX. upgrade to a 486DX? Intel has reconfigured the pins on the 486SX, strong need for the math coprocessor not just scrap the 486SX and So why wouldn't the owner of a 486SX computer who finds a

mium in the fast-growing segment of notebook computers (Seymour, mounted without a socket, thereby freeing up space that is at a prethe microprocessor small enough to be "surface mounted," that is, sors in 1991, and began removing the coprocessor. Intel could make Intel ceased to manufacture 486SXs with disabled math coproces-

2.2 IBM LASERPRINTER E

ppm for the LaserPrinter. According to Jones (1990), the LaserPrinter E uses the same "engine" and virtually identical parts, with one exa lower cost alternative to its popular LaserPrinter. The LaserPrinter E model printed text at 5 pages per minute (ppm), as opposed to 10 In May 1990, IBM announced the introduction of the LaserPrinter E, was virtually identical to the original LaserPrinter, except that the

that it can market it at a lower price. inserts wait states to slow print speed. . . . mounted chip. PC Labs' testing of numerous evaluation tue of four socketed firmware chips and one surface to some expense to slow the LaserPrinter in firmware so units indicated that the LaserPrinter E firmware in effect The controllers in our evaluation unit differed only by vir-IBM has gone

the machine pause and hence print more slowly. Moreover, this is counters or idlers, chips that perform no function other than to make IBM has added chips to the LaserPrinter E that serve as

applies to text printing, so that graphics comes out at the same speed. the only difference in the two machines. In particular, the idling only

It is interesting that *PC Magazine* (Jones, 1990) gave a good review of the LaserPrinter E, calling it "the obvious choice" over the Hewlettcost of the upgraded LaserPrinter E to \$200 more than the original E to identical performance with the LaserPrinter, bringing the total Packard IIP. For an additional \$1099, one can upgrade the LaserPrinter

2.3 SONY MINIDISCS

now being introduced on standard Compact Disc players. applications. Sony accomplished this by inserting a memory buffer the interruption of music caused by shock or vibration in portable MiniDisc is not only smaller than a regular CD but is also immune to audio Compact Disc onto a disc which is only 2.5 in. in diameter. The compression algorithm that permits squeezing the content of an entire provide 74 minutes of music, Sony's engineers devised a data small format, not its sound quality or durability) and still be able to necessary for success (the audio cassette's popularity derives from its tended to replace the analog audio cassette, but offering greater con-Sony recently introduced a new digital recording-playback format inbetween the laser pickup and the digital decoding circuitry, a feature venience and durability. To achieve the small form factor deemed

nism able to read both types of discs (intended primarily for portable complementary hardware that either includes just a playback mechaas the prerecorded discs, but uses a technology originally developed fore entirely optical. The recordable variety looks externally the same encoded on the surface of the disc; its principle of operation is therelike its bigger brother, it uses a laser beam to read the information corded variety is essentially a miniature CD housed in a plastic shell: and come in two varieties: prerecorded and recordable. The preretended primarily for home use). or in-car use), or both a recording and a playback mechanism (infor computer data storage: magneto-optical recording. ⁶ Sony produces MiniDiscs are similar in appearance to 3.5 in. computer diskettes,

own label. Blank MDs come in two varieties: 60-minute discs and 74below CDs. Some 400 titles are currently available, mostly from Sony's Prerecorded MDs are priced in the same range, but slightly

^{6.} For a (1992, 1994). For an in-depth discussion of the technology underlying MiniDiscs, see Harley

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\$16.99. Despite the difference in price and recording length, the two minute discs. The list prices for these discs are currently \$13.99 and formats are physically identical:

there's room on the media. (Harley, 1994) and prevents recording beyond this length, even though A code in the table of contents identifies a 60-minute disc The 60- and 74-minute discs are identical in manufacture

has made this nearly impossible: constructing a device that alters the table of contents. However, Sony One might think that a clever user could circumvent this scheme by

how much recording time is available. (Harley, 1992) information encoded in the lead-in area: it tells the player 74-minute disc and blanks of shorter playing time is the the disc playback time. . . . The only difference between a which includes the optimum laser power for recording and MD recorder reads the information in this un-erasable area, "lead in," has pits impressed in it just as on a CD. at the inner radius is left uncoated. This area, called the thin layers of magnetic material. A ring of polycarbonate Blank MDs are polycarbonate substrates coated with very

Sony already has plans to make the technology available for computer storage. An MD data disk will have a maximum capacity of 128 Mb.

2.4 TONTINES

upon his own life. Meanwhile, by selling the annuities to a large submodern annuities, anyone could be named as the nominee. This effecand receive interest as long as the nominee remained alive. Unlike returns. The purchaser of such an annuity would name a nominee, turn, the governments also issued life annuities carrying much higher to relatively riskless government bonds yielding a normal rate of renot so much their maturity structure as their risk structure. In addition debt instruments. Interestingly, what differentiated the liabilities was large government deficits that were financed with a variety of different eighteenth centuries. The frequent wars during this period produced governments widely used the practice during the seventeenth and uct is by no means a new phenomenon. In fact, the British and French While the above examples are all of recent vintage, crimping the prodprovided the annuitant with a random return uncontingent

tempt to price discriminate between individuals who differed in their tively government sponsored lotteries. However, the fact that private investment opportunities.8 Such random payout bonds disap-Smith and Villamil (1993) argue that tontines were created in an atdenominationssecurities paid higher interest rates and were only available in large that these annuities satisfied a desire for gambling, i.e., were effecscriber base, the government faced little or no risk. 7 It might be argued Kurdistan is apparently offering them today.9 peared as investment and saving opportunities increased, although -indicates that they were inferior commodities. Interestingly, -approximately the average annual income of the

OTHER EXAMPLES

of other examples of damaged production. easier to document. This subsection presents some brief summaries crimping the product is extremely pervasive in these industries, and concern electronics order to extract more revenue. Three out of the four examples above goods, since something seems wasteful about damaging a good in probably not surprising that manufacturers conceal damaged Or. computer hardware. This is no accident:

- late 1960s, IBM began to face strong competition in the disk drive drive to the computer and controls the actions of the spindle. In the second major component is the controller, which connects the disk read/write heads, and the actual spindle that the platter turns on. The components. The spindle includes the disk platter, a motor to turn it, orex offered a separate controller, which meant customers could pur-IBM's, which could be used with IBM controllers. In addition, Memcompanies, notably Telex and Memorex, offered spindles superior to market, which provided memory for the IBM 360 mainframe. 2.5.1 IBM 2319 Disk Drive: 10 A disk drive is composed of two major
- 7. In the case of a lottery bond, a bond with a random payout but without the annuity feature of tontines, offered by England, the bond was bundled with a lottery, and offered significantly higher average rates of return than bonds without lotteries, corresponding to a lower price. A tontine divides a fixed amount of money among the annuitants with surviving nominees, thereby being risk-free from the government's perspective, but risky from the individual's perspective.

 8. Section 6 of Smith and Villamii (1993), upon which the above discussion is based, contains a detailed discussion of the various types of debt instruments in use
- during this period, as well as an extensive bibliography.

 9. Source: conversations with Bruce Smith of Cornell University.
- McGowan, and Greenwood (1983). 10. This material is derived from DeLamarter (1986, Chapter 12), who worked as an economist for the DOJ in the famous IBM case. For a contrasting view, see Fisher,

as old customers. and thus IBM faced loss of disk drive sales for new customers as well dubbed Merlin, would not be ready for introduction for several years, more powerful than the old 360s, but its new disk drive system, frame. Worse still for IBM, it had introduced the IBM 370 mainframe, chase Memorex disk drives and just plug them into the IBM main

a controller and a spindle to decode the controller communication interface as well, thus forcing any rival who wished to offer both controllers as well. To undercut Memorex, IBM changed the controller rivals' spindles. This, of course, didn't eliminate Memorex, which sold that could be plugged into the unit, and undercutting the market for into the single unit, thereby limiting the number of additional spindles controller, which was previously an outboard device (separate unit), IBM renamed its existing 2314 disk drive the 2319, and integrated the lard." According to DeLamarter (1986) this scheme worked as follows: scheme internally called "Apricot," a name later changed to "Mal-To protect the market for 370 disk drives, IBM introduced a

marter (1986): The extent of the price discrimination is summarized by DeLa-

widely different prices. Where IBM charged \$256,000 for eight unbundled 2314 spindles and a controller for use on the 360, a similar number of 2319 spindles along with the offering each group essentially the same product but at went for as little as \$145,415 file adaptor [changed controller] on a 370/135 processor IBM would favor 370 customers at the expense of 360 users,

a "gimicky tactic" to "buy time." IBM vice president P. W. Knaplund described the 2319 relabeling as

(1987, p. 186) reports: tronics products has proven harder to document. Nevertheless, Nagle disabled.11 Unfortunately, the use of this strategy in consumer electheir higher priced alternatives only by having some of the features calculators, video equipment, VCRs, and multitesters) differ from how lower priced models of consumer electronics (such as pocket tic in consumer electronics. We have heard numerous accounts of 2.5.2 Consumer Electronics: Crimping the product is a popular tac-

^{11.} For example, in an April 1993 internet message posted to the rec.video discus sion group, Terry Jeffery (UK) reported discovering undocumented features on his Cannon video-camera.

more than the nonprogrammable version. The only practicard programmable version of one calculator for much case of the programmable version where the cards could cal difference between the two was a slot in the plastic A leading manufacturer of pocket calculators . . be inserted

do not have the alternate functions imprinted upon them. 12 differs from the higher priced scientific version only in that its buttons calculator manufacturer, Sharp Electronics, produces a calculator that programmable version into a programmable version. Another leading ronics magazine printed an article explaining how to convert the non-We have been told (but were unable to verify) that a consumer elec-

MD strategy to that of the hand-held multimeter industry: Robert Harley, one of Stereophile's technical editors, likens Sony's

some of their features disabled. (Harley, 1992) out the product line; the less expensive models merely have industry. The same electronics are in every meter through-This is analogous to a trick of the hand-held multimeter

tries, as the next few examples demonstrate. puters, crimping the product occurs in a broad range of other indus-While deeply entrenched as a strategy in electronics and com-

some of their capability. We know of two examples.

Wolfram Research, Inc. 13 sells a student version of its popular put limiting factors into the full-featured versions, thus destroying ducing "student versions" or educational versions of software is to Educational Software: It appears that the normal way of pro-

mathematics program, Mathematica, for \$180, less than a quarter of have a coprocessor. 14 significantly slower. Mathematica requires a fairly powerful microof the math coprocessor makes some kinds of numerical calculations sor, even if one is present on the student's computer. This disabling ematica program with one exception: it does not use a math coprocesthe normal price. The student version implements the complete Mathcomputer to operate; most student users are therefore likely to already

^{12.} It could, however, be argued that some people may prefer not having access to the scientific functions: square root buttons only serve to confuse them.

13. The source for this material is conversations with Hal Varian, April 22, 1993.

is familiar with the marketing practices of Wolfram Research.

14. Removing the calls to the coprocessor is a simple task, which directly incurs an Varian has edited a book entitled Economic and Financial Modelling with Mathematica and

insignificant additional cost. However, some additional cost would arise from marketing and supporting two versions of the program.

student version, which has "reduced data handling capabilities," sells for the MacIntosh computer. The full retail version sells for \$95. 15 The for \$69.95 Data Desk is an exploratory data analysis and statistics package

specifically for this market. gether, to produce a minimum purchase larger than would normally ers have responded in two ways: by bundling a number of units to of course, undercut the normal grocery store market, and manufactur-Buying clubs specialize in large quantities. Purchases in these outlets market for many consumer items according to the quantity purchased. stores such as Sam's, Costco, and The Price Club has segmented the be demanded by even a large family, and by producing larger sizes 2 5 4 4 Buying Clubs: The proliferation of discount "buying club"

rate production runs for the warehouse market. (Larson, 1993). Other manufacturers, including Chinet (disposable Manufacturers turn to contract packagers to create multipacks "betableware) and Mrs. Paul's (fish sticks), design and manufacture sepacated in-house lines for filling or multipacking larger-size packages' cause they don't want the expense of designing and building dedi-Creating multipacks, or bundling, incurs additional cost directly

duced packages of 125 units for warehouse clubs, it introduced a 40 tionally, Chinet sold its products in packages of fifteen. Having introclub market siphoning off demand from retail grocery stores, and manutacturers are segmenting the market: count package for "economy aisles" in grocery stores. Nonetheless have responded by obtaining larger sizes from manufacturers. Tradi-Grocers are quite concerned about the growth of the warehouse

ounce. 16 it difficult for us to buy those items with a low price per blocks for wholesalers [who sell to retail grocers]; making With larger sizes, manufacturers are creating stumbling

Interestingly, packagers note the inefficiency of these large bundles associated with consumer sales:

shown. When we tracked it to the manufacturer, we were told that those items wern not made for our class of trade.... I might not need a three-pack of toothpaste bander together, but I want to know it's available" (p. 92). of the magazine is devoted to grocers grousing about competition from warehous clubs. Another adds "We have seen items in competitors' stores that we were no 15. Data Desk is produced by Data Description of Ithaca, NY. Prices are as of December 1991, as reported in *The Higher Education Product Companion*, Vol. 1, No. 1, p. 18. 16. Marty Rodgers, quoted in *Progressive Grocer*, May 1992, p. 86. Much of this issue

don't have room, or their family isn't big enough. So they a bundle of 24 rolls of paper towels themselves. Many warehouse shoppers have no intention of using, say, "team-buy" with a friend. Then they split up the multi-They just

ire efficient to assist in segmenting the market. This evidence is suggestive that manufacturers create larger sizes than

mimals don't need the vitamins) from switching. 18 ome bundled with vitamins, to deter the high value users (whose nave different values, and the medicine aimed for low value use may Even within veterinary use, medicines used for distinct animals may ines with vast price differences between human and veterinary use. lrinking the ethanol. The newspapers often contain stories of medizasoline to ethanol sold as automobile fuel to prevent people from seriously compromises the high value use. For example, Brazil added add an adulterant to the chemical sold for a low value use, which urer can reduce arbitrage. One method of reducing arbitrage is to offer an opportunity for price discrimination, provided the manufac-2.5.5 Chemicals: Distinct uses for a given chemical will generally

neans of damaging the product. and in one case, expended significant resources to compute the best s evidence that the manufacturer contemplated damaging the product, is that the manufacturer actually damaged the product. Instead, there In the following two examples, there is no evidence available to

(monomer) MM for \$22 per pound to licensed dental laboratories. pound, and a prepared mixture consisting of powder and liquid dered version of MM (polymer) for industrial uses at 85 cents per pricing policy certainly corroborates this claim: they sold the pow-Haas, followed a uniform price policy and acted as a cartel. Their Watkins (1947), the two manufacturers of MM, du Pont and Rohm & uses. It is also used to make dentures. According to Stocking and Methyl methacrylate (MM) is a plastic with a variety of industrial

The price difference was evidently too great, and attracted

to liquid, and sell the polymer and monomer together at a bootleggers who found they could crack the powder back profit to the dental trade. (Stocking and Watkins, 1947, p. 403; italics added)

^{17.} John Berkeley, quoted in Larson (1993).

^{18.} An imperfect example is cooking wine: this is ordinary wine with sufficient salt idded to make it undrinkable. Cooking wine is generally sold to avoid paying taxes ather than to screen out high value users. Originally, cooking wine was developed o solve the moral hazard problem associated with cooks drinking the wine.

Rohm & Haas suggested ited by the Food and Drug Administration for that use. A licensee of that it would be unsuitable for use in dentures and would be prohib-Rohm & Haas considered adulterating the powdered version so

them rear up. (Quoted by Stocking and Watkins, 1947, p. them [the FDA] to confiscate every bootleg unit in the coun-A millionth of one percent of arsenic or lead might cause try. There ought to be a frace of something that would make

MM (Nagle, 1987). strategy of planting a rumor that they had adulterated their powdered situation." However, Rohm & Haas did resort to the less effective although they called it "a very fine method of controlling the bootleg There is no evidence that Rohm & Haas put this policy into effect,

riorate rapidly, but not affect paint, were also considered. Finally nificant effect on paints. Compounds that would cause cotton to dete Three distinct strategies for contamination were considered. Ground colors that would render them suitable for paint but not for textiles iments to determine the feasibility of adding contaminants to the ted quite high prices. Both companies held conferences and ran experto market "Monastral" colors, used for both paints and textile dyeing nies, du Pont and General Aniline, possessed exclusive U.S. rights added, again to prohibit use in textile dyeing. compounds that would irritate glass would damage painting rolls used in textiles, but have an insig-The use in paints required low prices, while the use in textiles permit According to Stocking and Watkins (1947), two chemical compa skin and cause dermatitis could be

case, and those where there is a single use for the product, such as laser printers and microprocessors. We now turn to the welfare software, or paint dyeing for pigments), which we call the dual use ondary, low value use for the product (such as educational use ir ples naturally divide into two categories: those where there is a sec significantly reducing demand for the high quality good. The exam ate a lower quality good, which they may sell at a lower price withou implications of damaged goods in the dual use case. features, degrade performance, or otherwise damage products to cre As we have seen, manufacturers in many circumstances disable

3. THE DUAL USE CASE

There are two types of consumers, denoted X and Y, and a monopoly producer of two qualities, L and H, for low and high. Consumers buy

and good H are constant, and denoted by c_L and c_{H} . he monopoly prices on these demand curves by M_i^z , for $i \in \{L, H\}$ and $z \in \{x, y\}$. For example, M_L^x is the monopoly price associated with 300d, when this is the only version available for purchase. Similarly denote consumer X's demand for the low (respectively high) quality on which good yields the highest net surplus. Let x_L (respectively x_H) one good or the other, but not both, and base their purchase decision demand x_L . et y_L and y_H represent consumer Y's respective demands. We denote The monopolist's marginal cost of production of good L

cations discussed in Section 2: Our first set of assumptions ensures that the model fits the appli-

$$) \leq c_H \leq c_{L_{\prime}} \tag{1}$$

$$f_H(p) \ge y_L(p)$$
 and $x_H(p) \ge x_L(p)$, (2)

nd

$$(\forall p_L, p_H)$$
 $0 < \int_{p_L}^{\infty} x_L(p) dp \le \int_{p_H}^{\infty} x_H(p) dp$ $\Rightarrow \int_{p_L}^{\infty} y_L(p) dp < \int_{p_H}^{\infty} y_H(p) dp.$

nigh quality:19 the monopolist were required to sell only one quality, he would offer ooth types of consumers. Jointly, conditions (1) and (2) imply that if hat H is indeed the high quality good, with increased demand by ered, and hence more costly, version of H. Inequality (2) guarantees Inequality (1) just formalizes the notion that L represents an al-

$$\forall p \ge c_H$$
 $(p - c_L)[x_L(p) + y_L(p)] \le (p - c_H)[x_H(p) + y_H(p)].$

strictly prefers purchasing H^{20} This ensures that if the low quality sumer X weakly prefers purchasing H to purchasing L, consumer Yy is CS = $\int_p^{\infty} q(z) dz$. Thus, assumption (3) says that whenever con-Recall that the consumer surplus associated with demand q and price

However, while the theory applies to cases where $c_L < c_H$, these are economically not very interesting, for it is then no longer obvious that price discrimination is occurring, 19. This is the only place in our argument where we use assumptions (1) and (2). The conclusions of Theorem 1 remain valid if we impose the above condition directly, ncreasing the range of applicability beyond situations where (1) and (2) are satisfied

and less surprising that introducing L leads to a Pareto improvement. 20. There are various more primitive assumptions that can be imposed to imply condition (3). In particular, if either $x_L = x_H$ or $y_L = x_L$ and $y_H > x_H$ whenever $x_H > 1$, then (3) holds. Also, if inf $\{p \mid x_L(p) = 0\} = \inf\{p \mid x_H(p) = 0\}$ and if for all p_L , p_H such that $x_L(p_L) > 0$ we have $x_H(p_H) x_L(p_L) < y_H(p_H) y_L(p_L)$, then (3) is satisfied. None of these appear to improve on (3) directly, which [in conjunction with assumption (4) selow] is interpretable as stating that Y is more H loving than X.

good is introduced, it will be targeted towards the X segment of the market.

duction of good L is profitable, and produces a Pareto improvement Let $M_H^{xy} = \arg\max_p (p - c_H)[x_H(p) + y_H(p)]$. We assume that the Σ market is not served if the firm sells only one quality. That is, Our next set of assumptions serves to guarantee that the intro

$$\chi_H(M_H^{\chi_H}) = 0. (4)$$

nomically meaningful characterization. straints, but such a consideration does not appear to lead to an eco for H. This effect need not dominate the effects of the incentive con If (4) fails, then typically we have the monopoly price for both market thus introducing the L good will tend to increase the price charged falling between the monopoly prices for the markets individually, and

this out, we assume tend to make introducing the low quality good unprofitable. To rule prefers the L good over the monopoly price for the H good: This wil willing to purchase a positive quantity of the L good, the Y consume It is possible that, at any price for which the X consumer is

$$\int_{M_H^y}^{\infty} y_H(p) dp \ge \int_{\overline{p}_L}^{\infty} y_L(p) dp. \tag{5}$$

ing H at the monopoly price to purchasing L at the price \overline{p}_L , the lowes price for which the X demand for L is zero. The inequality (5) ensures that the Y consumer would prefer purchas

provement. duce the low quality good L, and its introduction is a Pareto im Under these assumptions, the firm will always choose to intro

Then the introduction of the good L is a Pareto improvement. If, in addition THEOREM 1 Suppose that (1)–(5) hold, and suppose that $x_L(c_L) > 0$

$$\int_{M_H^y}^{\infty} y_H(p) \, dp < \int_{M_I^x}^{\infty} y_L(p) \, dp, \tag{6}$$

then the improvement is strict: all three agents strictly benefit

All proofs are contained in the Appendix.

creased to deter him from buying the inferior good. then the high demand type benefits as well, because his price is de tive constraints on the high demand type bind at the monopoly prices benefits the low demand type and the firm. If, in addition, the incen good is introduced, then the introduction of the low quality If the low demand L type is not served when only the high quality Theorem 1 captures the intuition provided in the introduction

(demand curves or both Y demand curves. As a result, provided listinct agents of the X type and many agents of the Y type. I market, the existing theory applies to the case where there are many A_H^{xy} stays sufficiently high that the X types remain excluded from the The assumptions (1-3) and (5-6) are invariant to rescaling both

ontinuum of consumer types, rather than two distinct markets. nicroprocessor and the IBM LaserPrinter E seem best modeled by a 10 less and education would seem to fit this model. In contrast, the hemical products, pharmaceuticals, and software used for both busin the previous section. The key question is whether the low demand ype would be served in the absence of the lower quality good. Thus, Theorem 1 seems relevant for several of the examples discussed

4. THE SINGLE USE CASE

issume v has cumulative distribution function F, good to a type v consumer is $\lambda(v)$. We assume lensity f, and that F has support [a, b]. The value of the low quality ndex the consumers by the value v of the high quality good. We with continuous

$$\lambda(a) \le a \quad \text{and} \quad (\forall v) \quad 0 \le \lambda'(v) < 1.$$
 (7)

ng with the applications previously discussed, we also assume²¹ good and constant marginal cost c_L for the low quality good. In keep-The monopolist has constant marginal cost c_H for the high quality

$$1 \le c_H \le c_L < b. \tag{8}$$

given by 1 - F(p), and that the demand for the low quality good at ity, it produces high quality: assumptions (7) and (8) imply that if the firm produces only one qualprice p is given by $1 - F(\lambda^{-1}(p))$. Consequently, as in Section 3, Note that the demand for the high quality good at price p is

$$(\forall p \ge c_H)$$
 $(p - c_H)[1 - F(p)] \ge (p - c_L)[1 - F(\lambda^{-1}(p))].$

satisfy When offering only high quality, the profit maximizing price p_1 must

$$0 = p_1 - c_H - \frac{1 - F(p_1)}{f(p_1)}. (9)$$

^{21.} Forcing $c_H \ge a$ is convenient to ensure an interior solution to the firm's maximization problem, but not necessary. In particular, it is possible to place assumptions directly on the inverse hazard rates used below.

usual hazard rate assumption, familiar in all adverse selection models: To ensure uniqueness of a solution to eq. (9), we employ the

$$(\forall x \in (a, b))$$
 $x - \frac{1 - F(x)}{f(x)}$ is increasing. (10)

We also assume that $\lim_{x\to b} [1 - F(x)]/f(x) = 0$. This is satisfied is F is analytic or if f(b) > 0. Conditions (8) and (10) then imply that a solution to eq. (9) exists and satisfies $a < p_1 < b$.

The condition for the low quality good, analogous to (10), will also prove useful. Selling only the low quality good, the firm earns

$$\pi_L(p) = (p - c_L)[1 - F(\lambda^{-1}(p))]. \tag{11}$$

mus,

$$0 = \frac{\partial \pi_L}{\partial p} = -\frac{f(\lambda^{-1}(p))}{\lambda'(\lambda^{-1}(p))} \left(p - c_L - \lambda'(\lambda^{-1}(p)) \frac{1 - F(\lambda^{-1}(p))}{f(\lambda^{-1}(p))} \right). \tag{12}$$

every $c_L \in (a, \lambda(b))$, we assume To guarantee that the profit function π_L has a unique maximum for

$$\lambda(v) - \lambda'(v) \frac{1 - F(v)}{f(v)}$$
 is increasing. (13)

by introducing L the seller necessarily cannibalizes some of his high quality market. Whether or not introducing L is profitable depends cient conditions under which he is willing to introduce *L*. the seller's optimization problem, and provide necessary and suffiupon the strength of these two opposing forces. We will now set up sumers into the market, and hence is potentially profitable. However, unserved, since $p_1 > a$. Introducing L can draw some of these confirm offers only high quality, some segment of the market remains We now turn to the case of two qualities. Note that when the

consumers. More precisely, let v_H be the consumer type who is indifferent between purchasing either good, 22 high valuation consumers, and low quality towards low valuation if both goods are offered for sale, high quality will be targeted towards in quality of H over L, $v - \lambda(v)$, is increasing in v. This ensures that By (7), the premium a consumer is willing to pay for the increase

$$v_H - p_H = \lambda(v_H) - p_L, \tag{14}$$

^{22.} The critical value v_H may lie outside the range [a, b], but profit maximization ensures that this will never happen in equilibrium.

not purchasing at all, 23 and let v_L be the type who is indifferent between purchasing L and

$$\jmath_L = \lambda(v_L).
 \tag{15}$$

[hen consumers in the interval [v_L , v_H] purchase L, and consumers v_H , v_H , v_H] purchase v_H , v_H

ypes of consumers making purchases rather than the prices directly: It is useful to express the monopolist's profits in terms of the

$$\pi = (p_{H} - c_{H})[1 - F(v_{H})] + (p_{L} - c_{L})[F(v_{H}) - F(v_{L})]$$

$$= [v_{H} - \lambda(v_{H}) + \lambda(v_{L}) - c_{H}][1 - F(v_{H})] + [\lambda(v_{L}) - c_{L}]$$

$$\times [F(v_{H}) - F(v_{L})]$$

$$= [v_{H} - \lambda(v_{H}) + c_{L} - c_{H}][1 - F(v_{H})] + [\lambda(v_{L}) - c_{L}][1 - F(v_{L})].$$
(16)

outcome. π subject to $a \le v_L \le v_H \le b$. If $v_L = v_H$, then π gives the one quality That is, we can view the firm's maximization problem as maximizing

If v_L $< v_H$, the first order conditions for maximizing

$$0 = \lambda(v_L) - c_L - \lambda'(v_L) \frac{1 - F(v_L)}{f(v_L)}, \tag{17}$$

$$v_H - c_H - \frac{1 - F(v_H)}{f(v_H)} = \lambda(v_H) - c_L - \lambda'(v_H) \frac{1 - F(v_H)}{f(v_H)}.$$
 (18)

and the left-hand side of (18) is zero, in accordance with (9). In order tions (17) and (18) yields a global profit maximum:²⁵ condition, which also ensures that a solution to the first order condito ensure a unique solution for v_H , we need the following regularity = v_H , then the right-hand side of (17) must be nonpositive,

$$v - \lambda(v) - [1 - \lambda'(v)] \frac{1 - F(v)}{f(v)}$$
 is increasing.²⁶ (19)

- outside this range produce zero quantities.

 24. Note that $\{v_L, v_H\}$ is a nontrivial interval if and only if $p_L < \lambda(p_H)$.

 25. When $c_L < a$, a variety of other cases emerge. The possible solutions to these cases are as follows: (i) $a = v_L = p_1 = v_H$, (ii) $a = v_L = p_1 < v_H$, and (iii) $a = v_L < p_1 \le v_H$. In case (i), the low quality good is not introduced. In case (iii), $p_H > p_{I_L}$ and high $v_L > v_H > v_H$ and $v_L > v_H$ and $v_L > v_H$ and $v_L > v_H$ and $v_L > v_H$ are worse off when the low quality good is introduced. Case (iii) requires further
- assumptions to make a Pareto comparison. assumption (19) is equivalent to the remarkably 26. Provided f is differentiable, the assumption (19) is equivalent to the remarkably weak condition $(\partial/\partial v)$ $[1 \lambda'(v)][1 F(v)]^2/f(v) < 0$. By (10), then, (19) holds if λ is convex, or not too concave

Under these conditions, we have:

LEMMA 1 Suppose eqs. (7)–(19) hold. Then introducing L is profitable if and only if

$$\lambda(p_1) - c_L - \lambda'(p_1) \frac{1 - F(p_1)}{f(p_1)} > 0.$$
 (20)

the welfare consequences of introducing good L. improvement. The next lemma provides some immediate insights into turn to the conditions under which introducing L produces a Pareto Henceforth, we will therefore assume that (20) holds. We now

LEMMA 2 Suppose (7)–(20) hold. Then
$$v_L < p_1 < v_H < b$$
.

strictly better off. Obviously, by (20), the monopolist benefits as well then high valuation customers are made better off as well. low quality good makes consumers with valuations in (v_L, p_1) always relative to selling only the high quality. Note that introducing the to more consumers but sells fewer units of the high quality good, A Pareto improvement therefore occurs if and only if $p_H \leq p_1$, for Lemma 2 shows that, selling two qualities, the monopolist sells

strictly better off. tions below v_L (who do not get to purchase under either scenario) are $< p_1$, so that all market participants other than consumers with valua-The next result provides conditions sufficient to ensure that p_H

THEOREM 2 Suppose that (7)–(20) hold, that [1 - F(v)]/f(v) is nonincreasing, and that $\lambda'(v)$ [1 - F(v)]/f(v) is nondecreasing. Then $p_H < p_1$, that is, introducing the low quality good is a Pareto improvement.

not vacuous, as the following example demonstrates. The hypotheses of Theorem 2, in conjunction with (7)–(21), are

Example 1: Let $F(v) = 1 - e^{-(v-a)/\alpha}$ for v > a, with $b = \infty$, and $\lambda(v) = \beta v + e^{-\beta v} + (1 - \beta)a - e^{-\beta a}$. The parameters are assumed to satisfy $a < c_H + \alpha$, $(1 + \alpha\beta)e^{-\beta a} < 1$, and

$$c_H \le c_L < \beta [c_H + (1 + \alpha \beta)e^{-\beta(c_H + \alpha)}] + (1 - \beta)a - e^{-\beta a}.$$

are strictly satisfied, and thus are robust to perturbations in a smooth These are satisfiable if β is near zero and $\alpha > 1$. All of the assumptions

of the environment, as the next result shows. dual use case. Indeed, assumption (20) fails for many specifications ment for the single use case are much more stringent than for the Nevertheless, the conditions guaranteeing a Pareto improve-

LEMMA 3 Suppose $\lambda(v)/v$ is nondecreasing. Then (20) fails

strategy, clearly most goods sold are not intentionally damaged by we won't ever observe a good damaged to produce a lower quality percentage of all goods sold, but still on a large number of goods. the manufacturer. Thus, it may be that (20) only holds for a small good. In spite of the large number of examples of the use of this This makes (20) seem somewhat unnatural. However, when (20) fails, convex λ is a sufficient condition for (19) to hold (see footnote 26). convex, for that implies the hypothesis of Lemma 3. Recall that a A sufficient condition for (20) to fail is that $\lambda(0)=0$ and λ is

entiable, and let \bar{c}_L just make (20) fail, that is, which a Pareto improvement occurs. Suppose f is continuously differpremature. That this is not the case is shown by our next result. For cient rather than necessary, and hence that the above conclusion is "large" c_L , we have an exact characterization of the conditions under It might be countered that the conditions of Theorem 2 are suffi-

$$\bar{c}_L = \lambda(p_1) + \lambda'(p_1) \frac{1 - F(p_1)}{f(p_1)}$$

Then we have

THEOREM 3 For c_L close to \bar{c}_L , one has $p_H < p_1$ if and only if λ is convex.

assumption (4) implies that lowering the price of good H below its monopoly price will not cannibalize profits from the L market. In in the dual use case. The intuition is as follows. In the dual use case, longer necessarily profitable. Technically, the first order effect of a This has two consequences. First, introducing the L good is now no lowering the price of good H necessarily results in cannibalization.²⁷ the single use case, whenever the L good has positive market share, improvement are so much more stringent in the single use case than unprofitable. The reader may wonder why the conditions for a Pareto as shown in Lemma 3, convexity of λ tends to make introducing La Pareto improvement harder to achieve. lower price of good L is now more likely to be a price increase, making Secondly, because of the cannibalization, the optimal response to a reduction in the price of good H is no longer zero (it is negative). Thus, convexity of λ is necessary for a general result. However,

27. The single use model also differs from the dual use model in that individual demand is inelastic (up to the reservation price). Introducing unit demand into the dual use model produces qualitatively similar results to the general dual use case; thus the distinction between the two cases appears to have more to do with discrete types versus a continuum of types than with downward-sloping demand.

5. CONCLUSION

discount stores, as we recall from our graduate student days find the defects in apparel products labeled as "seconds" and sold ir low value use, such as farming, commences. It is often impossible to seem to dictate, as the rent gradient would appear to bottom out once located much farther away from major cities than land prices would practice is much more widespread. For example, outlet malls are often many of our examples are in chemicals and electronics, we think the of an inferior product or produce the product separately. Although to produce a lower quality product, rather than improve the quality the market and price discriminate is to damage an existing produc For many products, it appears that the cost effective way to segment 28

absent price discrimination, the high value market is more profitable improvement are not severe, and boil down to the assumption that In this case, the conditions for price discrimination to be a Pareto category, along with business versus educational uses of software markets (Sec. 3). Most of the chemicals and pharmaceuticals fit this a low value use, and this case seems best modeled as two distinct characteristics. In one case, there are two uses, a high value use and ing goods naturally divides into two distinct cases based on customer than the low value market. We have argued that the phenomenon of manufacturers damag

nation to produce a Pareto improvement seem more severe and unnat to fit this category. This case seems more naturally modeled with a continuum of use values. The restrictions necessary for price discrimifor the two products. Most of the electronics examples would seem products, but rather a group of consumers with distinct use values In the second case, there are not two separate markets for the

examples that quality is endogenous. For example, the slowdown of not only of quantity but also of quality. It is clear from some of the over all possible qualities, and firms' costs, which are now a function of the mathematical description of preferences, which must be defined quality of the inferior good, mainly because of the resulting complexity In modeling the phenomenon, we have not endogenized the

houses might seem like an example of damaging goods, but has an alternative, compelling explanation. Many upscale retailers, such as Neimann-Marcus, accept returns of high fashion clothes without a receipt. If the same item could be purchased unblemished at a discounter, it would not be possible for the upscale retailers to accept returns without proof of purchase, to the annoyance of their customers. Consequently, manufacturers rip labels or mark through them, as a signal that the item was sold by a discounter of their customers. The obliteration of manufacturers' tags for high fashion clothes by discount

ppear to be an interesting, if daunting, research goal ions for a Pareto improvement when quality is endogenous would he IBM LaserPrinter was chosen by IBM. Characterizing the condi-

with a price cut. This should have the effect of further undercutting the market for the nore competitive, thereby reducing prices for the slower printers. omparable to the IIP, IBM makes the market for the slower printers products were significantly differentiated. By introducing a product vas significantly faster than the Hewlett-Packard IIP, and thus the arly in the LaserPrinter case. In this case, IBM's regular LaserPrinter ompetition by another producer. This is difficult to explain, particuaster printer, as Hewlett-Packard responds to IBM's LaserPrinter E BM LaserPrinter E, appear to have been introduced in response to At least two of the damaged goods, the Intel 486SX and the

in unlikely explanation for IBM's behavior. ent the introduction of the LaserPrinter E. Nevertheless, this seems grow, admitting some equilibria with higher profits than existed abnachine. Thus, the set of equilibria to the repeated pricing game may large percentage of HP's sales by aggressive pricing, but it limits he cost of such punishment by permitting higher prices on the faster ion of the similar product. Not only does IBM gain the ability to take Tewlett-Packard for competitive pricing is enhanced by the introduc-It is possible as a theoretical matter that IBM's ability to punish

selves to be of high quality because of experience with the industry nelp and product updates, and more likely for the products themacturers to offer a full line of products. Offering a full line clearly irms seems warranted. Further research into price discrimination by imperfectly competitive ess likely to exit, more likely to support the products with technical nakes consumers feel more comfortable, perhaps because the firm is An alternative explanation involves the perceived need of manu-

APPENDIX: PROOFS

Proof of Theorem 1. irm solves the following maximization problem: o Y and L to X. Let p_H be the price of H and p_L be the price of L. The From (3), if the firm sells both goods, it sells H

$$\max_{p_H, p_L} (p_L - c_L) x_L(p_L) + (p_H - c_H) y_H(p_H)$$
 (P)

subject to

$$\int_{p_{\mathrm{H}}}^{\infty} y_{\mathrm{H}}(p) \, dp \ge \int_{p_{\mathrm{L}}}^{\infty} y_{\mathrm{L}}(p) \, dp, \tag{IC}_{y}$$

$$\int_{p_{\mathrm{H}}}^{\infty} x_{\mathrm{H}}(p) \, dp \le \int_{p_{\mathrm{L}}}^{\infty} x_{\mathrm{L}}(p) \, dp. \tag{IC}_{x}$$

and (5), IC_y is satisfied. This deviation increases profits when Δp_L is (5) we may assume that $p_L^* = \overline{p}_L$. Consider the following deviation: $p_L = p_L^* + \Delta p_L$, $p_H = p_H^* + \Delta p_H$. Choose $\Delta p_L < 0$, and let Δp_H be determined as follows. If IC_x does not bind, let $\Delta p_H = 0$. If IC_x binds, sufficiently small, for choose Δp_H so that IC_x holds with equality. In either case, by (3) Let (p_H^*, p_L^*) solve (P). First, note that $x_L(p_L^*) > 0$. Suppose by way of contradiction that $x_L(p_L^*) = 0$. Then $p_H^* = M_H^* = M_H^*$, and by

$$\frac{\partial \pi}{\partial p_L} \bigg|_{p_L = \overline{p}_L, p_H = M_H^y} = \left[(M_H^y - c_H) y_H^{\prime} (M_H^y) + y_H (M_H^y) \right] \frac{dp_H}{dp_L} \\
+ (\overline{p}_L - c_L) x_L^{\prime} (\overline{p}_L) + x_L (\overline{p}_L) \\
= (\overline{p}_L - c_L) x_L^{\prime} (\overline{p}_L) < 0.$$

ities: either IC_y does not bind, or it does [which occurs when (6) holds]. Then (3) implies IC_y does not bind, implying that $p_H^* = M_H^y$, which implies that IC_x does not bind by (4). There are two remaining possibil-This contradicts the hypothesis that (p_H^*, \bar{p}_L) solved (P). That $x_L(p_L^*) > 0$ implies IC_x does not bind. For suppose it does.

only offers one quality. better off, and Y obtains the same (monopoly) price as when the firm If IC_y does not bind, then $p_H^* = M_H^y$, so both X and the firm are

eto improvement occurs and all three agents benefit. lowering both prices increases profits. Hence if (6) holds, a strict Par-Now suppose IC_y binds, that is, (6) holds. It must therefore be the case that $p_H^* < M_H^y$, for $p_H^* \ge M_H^y$ and (6) imply $p_L^* > M_L^*$, and

Proof of Lemma 1. Suppose that

$$\lambda(p_1) - c_L - \lambda'(p_1) \frac{1 - F(p_1)}{f(p_1)} \le 0,$$

and that $v_H > v_L$. Then by (17) and (13) we have $v_L \ge p_1$, so $v_H > p_1$.

$$\frac{\partial \pi}{\partial v_H} = f(v_H) \left[-\left(v_H - c_H - \frac{1 - F(v_H)}{f(v_H)}\right) + \left(\lambda(v_H) - c_L - \lambda'(v_H) \frac{1 - F(v_H)}{f(v_H)}\right) \right].$$

and by (19)

$$\frac{1}{f(v_H)}\frac{\partial \pi}{\partial v_H}(v_H) < \frac{1}{f(p_1)}\frac{\partial \pi}{\partial v_H}(p_1).$$

The hypothesis and (9) then imply that

$$\frac{\partial \pi}{\partial v_H}(p_1) \leq 0,$$

contradicting that v_H is chosen optimally.

Conversely, suppose that
$$\lambda(p_1) - c_L - \lambda'(p_1) \frac{1 - F(p_1)}{f(p_1)} > 0,$$

and that $v_H = v_L$. Then $v_L = v_H = p_1$, and so

$$\frac{\partial \pi}{\partial v_L}(v_L) = -f(v_L) \left(\lambda(v_L) - c_L - \lambda'(v_L) \frac{1 - F(v_L)}{f(v_L)} \right) < 0,$$

contradicting that v_L is chosen optimally.

Proof of Lemma 2. If $v_L = v_H$, then $v_H = p_1$, and by (20)

$$\frac{\partial \pi}{\partial v_L} = -f(p_1) \left(\lambda(p_1) - c_L - \lambda'(p_1) \frac{1 - F(p_1)}{f(p_1)} \right) < 0.$$

 $v_H - c_H - \frac{1 - F(v_H)}{f(v_H)} = \lambda(v_H) - c_L - \lambda'(v_H) \frac{1 - F(v_H)}{f(v_H)}$ Thus $v_L < v_H$. By (13) and (17), $v_L < p_1$. Therefore, by (13) and (18), $> \lambda(v_L) - c_L - \lambda'(v_L) \frac{1 - F(v_L)}{f(v_L)} = 0.$

By (9) and (10), $v_H > p_1$. Finally, if $v_H = b$ and if f(b) > 0, then by (7) and (8)

 $\frac{\partial \pi}{\partial v_H}(b) = f(b) \left[-b + c_H + \lambda(b) - c_L \right] < 0.$

 $\frac{\partial \pi}{\partial v_H}(v_H) < 0$ If $v_H = b$ and f(b) = 0, then $\lim_{x\to b} [1 - F(x)]/f(x) = 0$ implies that

for some neighborhood around
$$b$$
. In either case, this contradicts the optimality of v_H .

Proof of Theorem 2. By (9), (15), (17), (18),

$$\begin{aligned} p_{H} - p_{1} &= v_{H} - \lambda(v_{H}) + \lambda(v_{L}) - p_{1} \\ &= \frac{1 - F(v_{H})}{f(v_{H})} \left[1 - \lambda'(v_{H}) \right] + \lambda'(v_{L}) \frac{1 - F(v_{L})}{f(v_{L})} - \frac{1 - F(p_{1})}{f(p_{1})} \\ &= \left(\frac{1 - F(v_{H})}{f(v_{H})} - \frac{1 - F(p_{1})}{f(p_{1})} \right) \\ &- \left(\lambda'(v_{H}) \frac{1 - F(v_{H})}{f(v_{H})} - \lambda'(v_{L}) \frac{1 - F(v_{L})}{f(v_{L})} \right) < 0, \end{aligned}$$

by the monotonicity assumptions and Lemma 3.

Proof of Theorem 3. First note that (17) implies

$$\frac{\partial v_L}{\partial c_L} = \frac{1}{\lambda'(v_L)} \left[2 + \frac{1 - F(v_L)}{f(v_L)^2} f'(v_L) - \frac{\lambda''(v_L)}{\lambda'(v_L)} \frac{1 - F(v_L)}{f(v_L)} \right]$$

and

$$\frac{\partial v_H}{\partial c_L} = \frac{-1}{[1 - \lambda'(v_H)] \left[2 + \frac{1 - F(v_H)}{f(v_H)^2} f'(v_H) + \frac{\lambda''(v_H)}{1 - \lambda'(v_H)} \frac{1 - F(v_H)}{f(v_H)}\right]}$$

Thus, evaluating at $c_L = \bar{c}_L$, we have $v_H =$ $v_L = p_1$ and

$$\frac{\partial p_H}{\partial c_L} \bigg|_{c_L = \bar{c}_L} = [1 - \lambda'(p_1)] \frac{\partial v_H}{\partial c_L} + \lambda'(p_1) \frac{\partial v_L}{\partial c_L}$$

$$= \frac{-1}{2 + \frac{1 - F(p_1)}{f(p_1)^2}} f'(p_1) + \frac{\lambda''(p_1)}{1 - \lambda'(p_1)} \frac{1 - F(p_1)}{f(p_1)}$$

$$+ \frac{1}{2 + \frac{1 - F(p_1)}{f(p_1)^2}} f'(p_1) - \frac{\lambda''(p_1)}{\lambda'(p_1)} \frac{1 - F(p_1)}{f(p_1)} .$$

 $\lambda(v)$. Thus, near \bar{c}_L , p_H falls as c_L is decreased if and only if λ is convex. By (13) and (19), this is positive if and only if $\lambda''(p_1) > 0$. That is, Proof of Lemma 3. $\lambda(v)/v$ is nondecreasing if and only if $v\lambda'(v) \ge$

$$\lambda(p_1) - c_L - \lambda'(p_1) \frac{1 - F(p_1)}{f(p_1)} \le \lambda'(p_1) \left(p_1 - \frac{1 - F(p_1)}{f(p_1)} \right) - c_L$$
$$= \lambda'(p_1) c_H - c_L < 0.$$

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